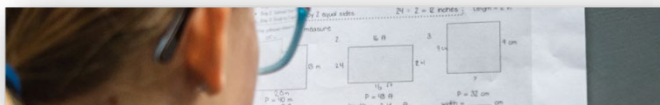


INFORMATION FOR EDUCATORS AND SCHOOL LEADERS

K-4 Foundational Mathematics Learning

PURPOSE

- The K-4 Math Foundational Learning Progressions (the Learning Progressions) help teachers navigate the curriculum and give guidance about what proficient students look like against the K-4 Math content Learning Standards.
- The Learning Progressions provide additional details and clarity for teachers about the Learning Standards in the Mathematics curriculum. While they are based on the curriculum, they do not replace it or teachers' professional expertise about using teaching strategies that best meet the needs of their students.
- The proficiency descriptors in the Learning Progressions align with the curriculum Learning Standards and learning goals for students at the end of the school year, from kindergarten to Grade 4. Teachers might use the Learning Progressions for planning, teaching and classroom assessment.



GUIDING INFORMATION

- Foundational mathematics skills, alongside the learning, practice, and demonstration of math curricular competencies and [cross-curricular Numeracy](#) experiences, support students in developing necessary Numeracy skills to become Educated Citizens.
- Most students develop along the proficiency scale continuum throughout the school year. Students may first be assessed as “emerging” or “developing” as they develop towards proficient in the foundational skills, as outlined by the high standards in the Learning Progressions.
- The K-4 Math Foundational Learning Progressions below are organized by skill. The Learning Progression Skills are Number Sense, Computational Fluency, Patterning and Algebraic Thinking, Geometry and Measurement, Data and Probability, and Financial Literacy. These skills align with and support the content learning standards of the Mathematics curriculum.

CURRICULUM-ALIGNED RESOURCES

- Teachers can use instructional strategies and learning resources recommended by professional associations, schools and districts, their own professional development, or outlined here, to help students develop toward end-of-year proficiency.
- See the [Teaching and Learning Stories](#) for examples of how current classroom teachers are supporting their students in developing cross-curricular Numeracy skills.
- **COMING SOON:**
 - Teaching and Learning stories showcasing foundational math skills – including samples of proficient student work
 - Further supporting resources in foundational mathematics and Numeracy instructional strategies in support of teachers' requests during the K-4 Foundational Learning Progressions Field Review



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Website: <https://curriculum.gov.bc.ca>

WHAT DOES MATH LEARNING LOOK LIKE IN THE CLASSROOM?

- Teachers are professionals who choose the strategies, resources, and applications best suited to the needs of students in their local setting (e.g., embedding mathematics in issues, projects, and passions relevant to the local community).
- Teachers can focus on “hands-on” experiential learning by incorporating the development of foundational skills through opportunities to encounter math in a wide variety of situational contexts. We encourage teachers to utilize instructional strategies in which students:
 - Reason mathematically to solve problems
 - Develop, demonstrate, and apply mathematical understanding through play, inquiry, and problem solving
 - Recognize that there are multiple ways to solve a problem and choose and use effective strategies and tools to solve problems
 - Communicate and reflect on their thinking process and solution using mathematical vocabulary
 - Engage in problem-solving experiences that are connected to place, story, cultural practices, and perspectives relevant to local First Peoples communities, the local community, and other cultures
- Observing, learning, and engaging in mathematical thinking empowers us to make sense of our world. Teachers who embed various ways of learning, practicing, and demonstrating mathematical knowledge and skills help students to develop as confident mathematicians who can enjoy and explore math and use math as a tool to unlock other areas of the curriculum.

OVERVIEW

Each **SKILL** represents the ability to demonstrate foundational mathematics knowledge. A proficient student should be able to develop, practice, and demonstrate each skill. All skills are important when building knowledge in mathematics.

Each **SKILL DESCRIPTOR** provides additional information as to the development within each **SKILL**.

Each **SUB-SKILL** further defines each skill.

The **DESCRIPTOR** is grade specific and describes what proficient student learning looks like at the end of the year/term.

| Grade 1 Mathematics Learning | |
|---|--|
| Skill - Number Sense | |
| Students with proficient Number Sense think flexibly and fluently. Number Sense is an understanding of numbers, ways of representing numbers, relationships among numbers, and making sense of numbers and quantities. It is developed through engaging in rich mathematical tasks in which students represent numbers in concrete, pictorial, and symbolic ways. | |
| Sub-skill | Proficiency Descriptor <i>(for the end of the school year)</i> |
| | Grade 1 |
| Whole Number Concepts <i>Students develop an understanding that numbers can represent a quantity. They also learn how to communicate with and about numbers. As students move to higher grades, they investigate relationships and patterns between numbers such as concepts of place value to be able to fluently add, subtract, multiply, and divide.</i> | For numbers up to 20: <ul style="list-style-type: none"> Accurately count (<u>stable order counting</u>): <ul style="list-style-type: none"> Forwards from 1 to 20 Backwards from 20 to 1 Forwards to 20 from different starting points <u>Skip count</u> by 2, 5, and 10, to 20 Compare and order numbers to make sense of quantities: <ul style="list-style-type: none"> Use relational language (e.g., more than, less than, equal to) Identify surrounding numbers using tools such as a number line or hundreds chart (e.g., less) Represent the number of objects in a set in <u>concrete, pictorial, and symbolic forms</u> (e.g., interlocking cubes, natural materials, loose parts, tally marks, or using a numeral), to make quantities Write the numbers 0-20 Instantly recognize the number of objects (<u>subitizing</u>) in sets up to 5 (e.g., images, objects) |

DEFINITIONS provide further explanation for key concepts found in the **foundational proficiency descriptors**.

Definitions

Note: Many of these terms are found in multiple aspects, sub-aspects, and grades. While the definitions are the same, in some instances the examples may vary due to the Aspect and Sub-aspect they are supporting.

2D shapes: includes but not limited to circle, square, rectangle, triangle, heart, kite

3D objects: includes but not limited to sphere, cone, cube, rectangular prism, triangular pyramid and square pyramid

Attribute: description of an element in a pattern, (e.g., colour, shape, size, number/letter/symbol, object, direction, position)

Bar graph: A way of showing numerical data by category using the height or length of a bar. Also known as a column chart. Bar graphs are used to compare things

Grade 1 Mathematics Learning

Skill - Number Sense

Students with proficient Number Sense think flexibly and fluently. Number Sense is an understanding of numbers, ways of representing numbers, relationships among numbers, and making sense of numbers and quantities. It is developed through engaging in rich mathematical tasks in which students represent numbers in concrete, pictorial, and symbolic ways.

| Sub-skill | Proficiency Descriptor <i>(for the end of the school year)</i> |
|---|---|
| | Grade 1 |
| Whole Number Concepts <i>Students develop an understanding that numbers can represent a quantity. They also learn how to communicate with and about numbers. As students move to higher grades, they investigate relationships and patterns between numbers such as concepts of place value to be able to fluently add, subtract, multiply, and divide.</i> | <p>For numbers up to 20:</p> <ul style="list-style-type: none"> Accurately count (stable order counting): <ul style="list-style-type: none"> Forwards from 1 to 20 Backwards from 20 to 1 Forwards to 20 from different starting points Skip count by 2, 5, and 10, to 20 Compare and order numbers to make sense of quantities: <ul style="list-style-type: none"> Use relational language (e.g., more than, less than, equal to) Identify surrounding numbers using tools such as a number line or hundreds chart (e.g., 1 more or 2 less) Represent the number of objects in a set in concrete, pictorial, and symbolic forms (e.g., using interlocking cubes, natural materials, loose parts, tally marks, or using a numeral), to make sense of quantities Write the numbers 0-20 Instantly recognize the number of objects (subitizing) in sets up to 5 (e.g., images, objects, dots, ten frame) |

Skill - Computational Fluency (Operations)

Students who are proficient in Computational Fluency understand how operations change numbers. Students are introduced to, learn, and practice math facts (fluent and automatized knowledge of addition/subtraction and multiplication/division equations), and build fact fluency. Students compute fluently by applying known math facts and through the practice of computational and mental math strategies. Students understand how to apply these foundational skills to solve contextual problems.

| Sub-skill | Proficiency Descriptor <i>(for the end of the school year)</i> |
|--|--|
| | Grade 1 |
| <p>Knowledge and Fluency of Math Facts</p> <p><i>Fact fluency (accurate, efficient and flexible knowledge of math facts) based on conceptual understanding (e.g., whole number concepts, place value concepts, and representing math facts in concrete, pictorial, and symbolic forms) is encouraged rather than memorization of discrete facts. Rote memorization of facts should not be prioritized at this level.</i></p> | <ul style="list-style-type: none"> • Compose and decompose sets up to 10 using concrete, pictorial, and symbolic forms (e.g., showing how 7 on a 10-frame can be made with 5 and 2 10-frames) • Use computational and mental math strategies such as counting on fingers to begin to learn math facts up to 10 • Explore a variety of activities such as games, discussions (e.g., a number talk of ways to make 7) and problem solving |
| <p>Understanding of Operations</p> <p><i>Understanding of operations builds on math fact fluency. It also requires an understanding of concepts such as place value to be able to add, subtract, multiply, and divide larger numbers beyond known math facts. The development and practice of various computational and mental math strategies builds flexibility in doing operations and applying these skills to solve contextual problems.</i></p> | <ul style="list-style-type: none"> • Compose and decompose sets up to 20 using concrete, pictorial, and symbolic forms to demonstrate understanding that addition brings sets of objects together and subtraction represents taking away from a set, or the difference between two amounts • Demonstrate understanding that addition and subtraction are related/opposite operations (e.g., show fact families such as $12 + 6 = 18$ and $18 - 6 = 12$ by connecting and disconnecting interlocking blocks) • Use computational and mental math strategies such as doubles, making groups of 10, and counting on from a starting number, to demonstrate understanding of addition and subtraction for numbers up to 20 • Solve contextual addition and subtraction problems <ul style="list-style-type: none"> ○ Choose the appropriate operation and strategy to solve a contextual problem ○ Explain their thinking using mathematical language (e.g., "I added the two sets because I needed to see how many I had all together.") |

Skill - Patterning and Algebraic Thinking

Students develop proficient Algebraic Thinking through recognizing patterns and trends, identifying and representing relationships between numbers, making generalizations, and analyzing change.

| Sub-skill | Proficiency Descriptor <i>(for the end of the school year)</i> |
|---|---|
| | Grade 1 |
| Patterning <i>Noticing relationships in patterns such as repetition helps students develop skills to observe, identify, and classify, and supports developing prediction skills.</i> | <ul style="list-style-type: none"> Identify the core of a pattern consisting of 3 to 5 repeating elements Describe attributes of repeating patterns to identify the pattern rule Represent a repeating pattern with 2 or more elements in concrete, pictorial, and symbolic forms (e.g., blocks, natural objects; shapes, letters; rhythms, movements) <ul style="list-style-type: none"> Represent pattern rules in symbolic forms, (e.g., using letter codes like ABABAB) Translate patterns from one representation to another (e.g., an orange-blue-orange-blue pattern could be represented by a clap-snap-clap-snap pattern) Predict an element in a repeating pattern |
| Algebraic Thinking <i>Students explore concepts and symbols of equality and inequality. They apply understanding of these ideas to solve for unknown values and understand relationships between numbers.</i> | <ul style="list-style-type: none"> Model equality as balanced and inequality as unbalanced using concrete and pictorial forms (e.g., comparing lengths of interlocking cubes) <ul style="list-style-type: none"> Make connections to ways to make 20 (Operations) (e.g., showing 2 rows of 10 blocks on one side and 20 blocks on the other) Demonstrate change tasks and explain reasoning Accurately use symbols of equality and inequality (= or \neq) Create accurate addition and subtraction equations for numbers up to 20 |

Skill - Geometry and Measurement (Spatial Sense)

Students develop strong Spatial Sense in part through the study of Geometry and Measurement and can demonstrate the ability to describe objects and position with mathematical language and numerical measurement.

| Sub-skill | Proficiency Descriptor <i>(for the end of the school year)</i> |
|---|--|
| | Grade 1 |
| 2D Shapes and 3D Objects <i>Noticing attributes of shapes helps students develop skills to observe, identify, classify, and supports creativity and design.</i> | <ul style="list-style-type: none"> Identify, describe, and sort 2D shapes and 3D objects using a single attribute and explain their thinking <ul style="list-style-type: none"> Compare and contrast shapes and design elements from various cultures, including local First Nations Use mathematical language to name and describe shapes (e.g., a triangle has 3 sides, a square has 4 corners) Compose and decompose larger 2D shapes by using smaller shapes (e.g., decomposing a hexagon into triangles) by drawing, or using digital technology or manipulatives like tangrams Recognize and identify similarities between 3D objects and begin to create 3D objects. (At this level, using specific mathematical terminology to name and identify 3D objects is not expected) Use mathematical language to describe attributes of shapes Identify 2D shapes and 3D objects in the real world (e.g., bentwood box, coins, longhouses, soccer ball, cans, steps in origami) |
| Measurement <i>Measurements iteratively use standard units (from established systems such as the metric system) and/or non-standard units (e.g., using hands or blocks to measure height). Mathematical language to describe position can be descriptive (qualitative) or numerical (quantitative). This sub-skill includes concepts of time.</i> | <ul style="list-style-type: none"> Use non-standard (uniform and non-uniform) and standard units to directly measure the length, width, or height of an object <ul style="list-style-type: none"> Accurately measure an object, edge to edge Use mathematical language to make direct qualitative comparisons between objects (e.g., bigger, smaller, longer, shorter, wider, narrower, heavier, lighter, holds more, holds less) and justify and explain their thinking Describe the position of objects qualitatively (e.g., up and down, in and out, to the right, to the left) |

Skill - Data and Probability (Data Literacy)

By developing proficient Data Literacy skills, students are able to demonstrate the ability to understand, analyze, and communicate data, and the ability to predict the likelihood of an event. As students move to later grades, they will use their foundational mathematics skills to collect, communicate, and discuss data across all areas of the curriculum.

| Sub-skill | Proficiency Descriptor <i>(for the end of the school year)</i> |
|--|--|
| | Grade 1 |
| <p>Understanding, Analyzing, and Communicating Data</p> <p><i>Graphs help to visually represent observations and data. Students build proficiency in collecting data to communicate in various types of graphs and inferring information from graphs.</i></p> | <ul style="list-style-type: none"> Collect and communicate data <ul style="list-style-type: none"> Record data using tally marks or manipulatives Communicate data using different representations (e.g., concrete graphs, bar graphs) Represent information on a concrete graph using one-to-one correspondence Interpret graphs using comparative language (e.g., more people like skipping than running) and direct language (e.g., 5 people like skipping) |
| <p>Probability</p> <p><i>Students discuss the likelihood of an event using descriptive language of probability. As students move to later grades, they will begin to use quantitative descriptors such as describing probability with fractions, decimals, and percentages.</i></p> | <ul style="list-style-type: none"> Describe the likelihood of a familiar event (such as the chance of snow) using age-appropriate probability language (never, always, sometimes, maybe, unlikely and likely) and explain their thinking |

Skill - Financial Literacy

Students with a strong understanding of Financial Literacy will develop the tools required to practice sound financial decision making in the future. This skill provides real world context for demonstrating learning in Number Sense and Computational Fluency.

| Sub-skill | Proficiency Descriptor <i>(for the end of the school year)</i> |
|---|---|
| | Grade 1 |
| Currency <i>Identifying, understanding the value of, and combining coins and bills fluently, with an emphasis on Canadian currency.</i> | <ul style="list-style-type: none"> Identify, name, and describe Canadian coins (nickels, dimes, quarters, loonies, toonies) by their size, design, and value Sort and count the number of different types of coins in a mixed set (connection to Number Sense) Use number sense strategies such as <u>skip-counting</u> to determine the value of a group of the same type of coin Calculate the total price (in whole numbers up to \$20) by adding and subtracting and by using representations such as price tags and play money (connection to Computational Fluency) |
| Financial Planning and Decision Making <i>Concepts of earning, saving, spending, and making financial plans and decisions.</i> | <ul style="list-style-type: none"> Role play financial transactions such as in a restaurant, bakery, or store. Explore trade games to understand that objects can have variable value or worth (tools, food, toys) Understand and explore concepts such as <ul style="list-style-type: none"> Roles, responsibilities, and jobs in the community (Career Education) Integrating the concept of needs and wants (Core Competencies) |

Definitions

Note: This is a complete list of foundational skill definitions from Kindergarten through Grade 4. Many of these terms are found in multiple Skills/Sub-skills and across grades. Therefore, the example included may or may not be appropriate for the grade.

2D shapes: includes but not limited to circle, square, rectangle, triangle, heart, kite

3D objects: includes but not limited to sphere, cone, cube, rectangular prism, triangular pyramid and square pyramid

Attribute: description of an element in a pattern, (e.g., colour, shape, size, number/letter/symbol, object, direction, position)

Bar graph: A way of showing numerical data by category using the height or length of a bar. Also known as a column chart. Bar graphs are used to compare things between different groups or to show data collected in different times or places.

Benchmarks: a familiar, measurable quantity used to help estimate or understand other quantities, (e.g., 5, 10, 100, 1000, 25, 50)

Cardinality: knowing that the last number said when counting represents the quantity of objects in a set

Change tasks: a task in which a student demonstrates changing a quantity using concrete, pictorial, and symbolic models (e.g., using blocks to show changing 8 to 12 by adding 4 more blocks)

Compose/Recompose: building or rebuilding a set of objects or a number from smaller parts. For example, 5 can be made from 1 and 4 or 2 and 3

Concrete forms: concrete materials or physical objects help students learn through actions such as placing, moving, grouping, or splitting objects. Examples include manipulatives (e.g., base-10 blocks, counters), natural or found materials, loose parts

Concrete graph: A graph that organizes and displays data using concrete objects like blocks or stickers, with appropriate labels.

Conservation: knowing that the number of objects remains the same despite changing the size of objects or how they are laid out

Contextual problem: a problem that is set within a real-world or practical situation, requiring students to apply mathematical concepts to solve it. Students identify and apply the best mathematical operation and strategy to fit the context, and based on their current knowledge and available tools

Core: repeated element in a repeating pattern, (e.g., AAB is the core of AABAABAAB)

Decompose: breaking down a number into smaller parts. For example, $12 = 10 + 2$, or 147 can be broken into 100, 40, and 7 OR 14 tens and 7 ones

Equivalents: quantities that are equal in value, function, amount, or meaning, but not necessarily number, i.e., 1 m = 100 cm, 4 quarters = 1 loonie

Estimate: to approximate a number, calculation, quantity, or measurement based on an educated guess, rounding, or a visual comparison with a referent or benchmark

Expanded form: breaking down numbers as the sum of the digits and their place value, (e.g., $123 = 100 + 20 + 3$)

Fact families: sets of related addition/subtraction or multiplication/division math facts such as $12 + 6 = 18$ and $18 - 6 = 12$, or $2 \times 7 = 14$ and $14 \div 7 = 2$. Fact families illustrate how sets can be decomposed and recomposed.

Fractions: numbers which can represent a part of a whole, part of a region, part of a set, or part of a length. The **denominators** of fractions represent equal-sized portions of a whole or unit. The **numerators** represent the number of portions within the fraction. For example, $\frac{2}{3}$ represents 2 portions (the numerator) out of a whole that has been divided into 3 portions (the denominator).

Irregular polygons: 2D shapes in which all sides are not equal in length or all angles not equal in measure

Many-to-one correspondence: On a concrete graph or pictograph, one symbol represents a group of objects (e.g., one square may represent five cookies)

Math facts: fluent and automatized knowledge of addition/subtraction and multiplication/division equations **One-to-one correspondence:** when counting the number of objects in a set, using one number per object for accuracy

Nets: representations of 3D objects if cut open and laid flat

Non-standard units: measurement units using everyday objects (e.g., a pencil, arm, shoe)

Non-uniform units: not consistent in size (e.g., children's hands, pencils)

Number pattern: also known as number sequences, are a series of numbers that follow a specific rule or have a relationship between successive numbers. Number sequences can be arithmetic (adding or subtracting by a constant, aka increasing or decreasing patterns. (e.g., 75, 70, 65, 60, 55, ...), or geometric (multiplying or dividing by a constant e.g., 1, 2, 4, 8, 16...)

One to one correspondence: On a concrete graph or pictograph, one picture symbol corresponds to one unit of data (e.g., one dot represents one flower)

Pattern rule: Pattern rules describe the relationship between elements in the pattern. Pattern rules can be based on attributes or mathematical operations. Patterns can be repeating, or number (increasing or decreasing) patterns.

Perimeter: total distance around the outside of a 2D shape. The perimeter of a circle is also called the circumference

Pictograph: A way of showing data using images, where each image stands for quantity (one to one correspondence or many to one correspondence). Pictographs are used to express large amounts of information in a simple manner as it is easy to read.

Pictorial forms: pictorial forms help students see a model which represents a number. Examples include pictures of counting collections, number lines, tally marks, 10-frames

Place value: the relationship between the digits within a number and their value, (e.g., the digit 4 in 49 has the value of 40)

Polygons: an enclosed 2D shape made up of straight lines

Preservation of shape: the orientation/position of a shape will not change its attributes but will change its appearance

Ratio table: a table to help understand the relationship between the quantities (e.g., a t-chart could record the total number of meals eaten at a camp, per day—one column could be the number of days, another column could be the number of meals). Ratio tables are also known as t-tables, function machines, or in and out machines

Referents: a known number of concrete or pictorial representations that can be used for comparison, to help estimate an unknown quantity. For example, a 10-frame (grid consisting of 2 lines of 5 squares) can be used as a referent for amounts less than or more than 5

Regular polygons: 2D shapes in which all sides are equal in length and all angles equal in measure

Skeletons: representation of a 3D shape without the faces

Skip counting: method of counting in which students add a number to the previous number (also known as multiples). For example, skip counting by 5, starting at 0 is 0, 5, 10, 15, ...

Stable order counting: accurately counting numbers in the correct sequence

Standard units: measurement units within established systems such as the metric system **Subitize:** instantly recognizing how many there are in a set without counting, e.g. knowing the number of dots on dice without counting. Subitizing can usually be done for a group of up to 5 objects

Symbolic forms: symbolic forms are abstract mathematical notations which represent numbers. Examples include numerals, tallies, musical notes, fractions

Symbols of equality and inequality: The = sign means “the same as”, e.g., $4 + 6 = 3 + 7$. Elements on both sides of the = sign are balanced regardless of size or shape. Symbols of inequality include less than < ; greater than > ; and not equal \neq

Uniform units: consistent in size (e.g., interlocking cubes, standard paper clips)

Unit fractions: fractions with 1 in the numerator, such as $\frac{1}{2}$ or $\frac{1}{5}$. They allow the comparison of the size of fractions (e.g., $\frac{1}{2}$ granola bar $>$ $\frac{1}{5}$ granola bar)

Computational and mental math strategies:

Addition and subtraction strategies

- **Compensating:** bridging to or decomposing to a benchmark or friendly number [ex: $47 + 28 \rightarrow$ add 3 to 47 to make 50 (friendly number) \rightarrow subtract 3 from 28 to compensate $= 25 \rightarrow 50 + 25 = 75$]
- **Commutative property:** the order of the numbers in an addition equation does not change the sum, (e.g., $3 + 5 = 5 + 3 = 8$)
- **Counting on and counting back:** starting from a number and counting on by the added number or back by the subtracted number
- **Decomposing:** breaking down a number into smaller or simpler parts to support computation. [ex: $47 + 28 \rightarrow$ decompose by place value: $47 = 40 + 7$; $28 = 20 + 8 \rightarrow$ add by place value: $40 + 20 = 60$; $7 + 8 = 15 \rightarrow$ add total: $60 + 15 = 75$]
- **Doubles:** e.g., $3 + 3 = 6$, $7 + 7 = 14$
- **Friendly numbers:** bridging to or decomposing to a benchmark or friendly number (ex. $7 = 5 + 2$, 5 is a “friendly number”). Often used in conjunction compensating, decomposing, or making 10/bridging over 10 strategies

- **Hundred Chart:** jumping along the hundred chart (similar to counting up and counting back) [ex: $47 + 28 \rightarrow$ Start at 47, add 20 (move 2 rows down) to 67, then add 8 (move 8 squares to the right) to 75]
- **Making 10/bridging over 10:** “bridging” to the nearest 10 (ex. $8 + 5$. The 8 can be “bridged” to 10 by adding 2 out of 5. Then, add the remaining 3 $\rightarrow 8 + 5 = 8 + 2 + 3 = 10 + 3 = 13$)
- **Open number line:** jumping along the number line (similar to counting up and counting back) [ex: $47 + 28 \rightarrow$ start at 47, jump 20 to 67, jump 3 to 70, jump 5 to 75]
- **Skip counting:** method of counting in which students add a number to the previous number. For example, skip counting by 5, starting at 0 is 0, 5, 10, 15, ...

Multiplication and division strategies: The strategies below utilize an understanding of place value and are encouraged. Traditional methods (e.g., long division) can rely on memorization of a procedure and may not effectively demonstrate a true understanding that multiplication is the addition of multiple groups (e.g., 12×2 is 2 groups of 10 and 2 groups of 2), and division is splitting a group into equal sized shares (e.g., $36 \div 3$ can be shown as $30 \div 3$ shares and $6 \div 3$ shares)

- **Decomposing:** breaking down a number into smaller or simpler parts to support computation (related to distributive property)
- **Distributive property (partial products):** a way to break down multiplication into smaller steps. Example: $5 \times 23 \rightarrow$ decompose 23 into 20 and 3 $\rightarrow 5 \times 23 = 5 \times 20 + 5 \times 3 = 115$